PAPER CODE - 8191 12th CLASS - 12022

TIME: 30 MINUTES MARKS: 20

MATHEMATICS

OBJECTIVE

OBJECTIVE MARKS: 20
NOTE: You have four choices for each objective type question as A, B, C and D. The choice which you think is correct, fill that circle in front of that question number. Use marker or pen to fill the circles. Cutting or filling two or more circles will result in zero mark in that question.

QUES	TION NO. 1
1	$\lim_{X \to +\infty} \frac{2-3x}{\sqrt{3+4x^2}} = \dots$
1 .	$x \to +\infty$ $\sqrt{3+4x^2}$ $(C) + \infty$ $(D) - \infty$
	$(A) 3/2 (B) -3/2 (C) + \infty (D) - \infty$
2	If $f(x) = \begin{cases} x + 2 & x \le -1 \\ c + 2 & x > -1 \end{cases}$ and $\begin{cases} \lim_{x \to -1} f(x) \text{ exists then } c = \dots \end{cases}$
	(A) -2 (B) 2 (C) 1 (D) -1
3	
3	$\frac{d}{dx} \sin h^{-1} x = \dots$
	(A) $\frac{1}{\sqrt{1+x^2}}$ (B) $\frac{-1}{\sqrt{1+x^2}}$ (C) $\frac{1}{\sqrt{1-x^2}}$ (D) $\frac{-1}{\sqrt{1-x^2}}$
4	Any point where function f is neither increasing nor decreasing provided $f(x) = 0$ is called
"	(A) Critical point (B) Point of inflection (C) Stationary point (D) Feasible point
_	3
5	$\frac{a}{dx}\cos(ax+b) = \dots$
	(A) $\sin (ax + b)$ (B) $-a \sin (ax + b)$ (C) $a \sin (ax + b)$ (D) $-\sin (ax + b)$
6	$\frac{d}{dx} e^{3x} = \dots$
	$(A) \frac{1}{3} e^{3x}$ (B) e^{3x} (C) $3 e^{3x}$ (D) $3 e^{3x} \ln 3$
7	$\int_{-\pi}^{\pi} \sin x dx = \dots$
	(A) -1 (B) 0 (C) 1 (D) cos x
8	$\int \frac{e^x}{e^{x+2}} dx = \dots$
	$(A) e^{x} + 3 + c$ (B) $e^{x} + c$ (C) $e^{x} \ln(e^{x} + 3) + c$ (D) $\ln(e^{x} + 3) + c$
9.	$\int \frac{x}{\sqrt{4+x^2}} \mathrm{d}x = \dots$
	$\begin{vmatrix} \sqrt{4+x^2} \\ (A) \sqrt{4+x^2} + c & (B) \frac{1}{2} \sqrt{4+x^2} & (C) \frac{1}{(x+4)^{3/2}} + c & (D) \ln \sqrt{4+x^2} + c \end{vmatrix}$
4.0	J
10	Solution of differential equation $\frac{dy}{dx} = -y$ is
	(A) $y = -ce^x$ (B) $y = ce^x$ (C) $y = ce^x$ (D) $y = e^x$
11	The distance between the points A (3, 1), B (-2, -4)
	(A) $2\sqrt{5}$ (B) $5\sqrt{2}$ (C) $\sqrt{5}$ (D) $\sqrt{2}$
12	The point of intersection of the lines $3x + y + 12 = 0$ and $x + 2y - 1 = 0$ is
	(A) $(5,3)$ (B) $(-5,-3)$ (C) $(5,-3)$ (D) $(-5,3)$
13	Slope of the line $2x + 5y - 8 = 0$ is
	(A) -2/5 (B) 2/5 (C) 5/2 (D) -5/2
14	The y-intercept of the equation of line $5x - 12y + 39 = 0$
	(A) $\frac{5}{12}$ (B) $\frac{-39}{12}$ (C) $\frac{39}{12}$ (D) $\frac{-5}{12}$
15	Graph of the inequality $x + 2y < 6$ lies
	(A) Opposite to origin (B) Toward origin (C) in 1st quadrant (D) in 2nd quadrant
16	Radius of the circle with equation $x^2 + y^2 + 2gx + 2fy + c = 0$ is
	(A) $\sqrt{g^2 + f^2 + c}$ (B) $\sqrt{g^2 - f^2 - c}$ (C) $\sqrt{g^2 + f^2 - c^2}$ (D) $\sqrt{g^2 + f^2 - c}$
17	The line through the focus and perpendicular to the directrix of parabola is called
	(A) tangent to parabola (B) axis of parabola (C) latusrectum of parabola (D) vertex of parabola
18	$x = a \cos\theta$, $y = b \sin\theta$ are parametric equations of
10	(A) Circle (B) Parabola (C) Ellipse (D) Hyperbola
19	If u and v be two vectors making an angle θ with each other then projection of $\underline{\mathbf{u}}$ along $\underline{\mathbf{v}}$ is
1	$(A) \ \frac{\underline{\underline{u}} \cdot \underline{\underline{v}}}{ \underline{\underline{v}} } (B) \ \frac{\underline{\underline{u}} \cdot \underline{\underline{v}}}{ \underline{\underline{u}} } (C) \ \frac{\underline{\underline{u}} \times \underline{\underline{v}}}{ \underline{\underline{v}} } (D) \ \frac{\underline{\underline{u}} \times \underline{\underline{v}}}{ \underline{\underline{u}} }$
20	$3\underline{j} \cdot \underline{k} \times \underline{i} = \dots$
	(A) 0 (B) - 3 (C) j (D) 3
L	14 (Obi)-12022-80000 SEQUENCE - 1 (PAPER CODE - 8191)

TIME: 2.30 HOURS

MARKS: 80

GROC		
		SECTION-I
QUES:	FION	NO. 2 Write short answers any Eight (8) of the following D44-61-22 16
	i	Prove the identity $\operatorname{sec} h^2 x = 1 - \tan h^2 x$
	ii	If $f(x) = 2x + 1$ and $g(x) = x^2 - 1$. The obtain the expression $fg(x)$
	iii	Obtain $f^{-1}(x)$ from $f(x) = -2x + 8$
	iv	Evaluate $\lim_{x \to 0} \frac{\sin x^{\circ}}{x}$
	L	If $f(x) = \begin{cases} x+2, & x \le -1 \\ c+2, & x > -1 \end{cases}$, find "c" so that $\lim_{x \to -1} f(x)$ exists
	vi	If $y = \left(\sqrt{x} - \frac{1}{\sqrt{x}}\right)^2$, then find $\frac{dy}{dx}$
	vii	Differentiate $x^2 - \frac{1}{x^2}$ w.r.t. " x^4 "
	viii	If $y = x^2 \sec 4x$, then find $\frac{dy}{dx}$
	ix	Obtain $f(x)$ from $f(x) = x^3 \cdot e^{1/x}$
E	х	Find $\frac{dy}{dx}$ if $y = x e^{\sin x}$
	xi	Determine the interval in which $f(x) = 4 - x^2$, $x \in (-2, 2)$ is increasing
	xii	Examine the function $f(x) = x^2 - x - 2$ for critical values

QUESTION NO. 3 Write short answers any Eight (8) of the following

i	Use differentials to find $\frac{dy}{dx}$ if $xy + x = 4$
ii	Find $\int \frac{dx}{\sqrt{x+1} - \sqrt{x}}$
iii	Find $\int x \cdot \sqrt{x^2 - 1} dx$
iv	Find $\int \frac{x^2}{x^2+4} dx$
·V	Find ∫ tan ⁻¹ x dx
vi	Find $\int e^{-x} (\cos x - \sin x) dx$
vii	$\int_{-6}^{2} \sqrt{3-x} dx$
viii	Solve the differential equation $\frac{dy}{dx} = \frac{y}{x^2}$
ix	Find the equation of a vertical line through (-5, 3)
х	Convert the equation $2x - 4y + 11 = 0$ (i) Two intercepts form (ii) Normal form
xi	Check whether the point (5, 8) lies below or above the line $2x - 3y + 6 = 0$
xii	Find the lines represented by $3x^2 + 7xy + 2y^2 = 0$

QUEST

TION	NO. 4 Write short answers any Nine (9) of the following 18				
i	Graph the solution set of $3x - 2y \ge 6$				
ii	Graph the solution set of the following linear inequality $3x + 7y \ge 21$, $y \le 4$				
iii	If $\underline{\mathbf{v}} = \frac{-\sqrt{3}}{2}\underline{\mathbf{i}} - \frac{1}{2}\underline{\mathbf{j}}$. then find a unit vector in the direction of $\underline{\mathbf{v}}$				
iv	If $\underline{\mathbf{u}} = 2\underline{\mathbf{i}} + 3\underline{\mathbf{j}} + \underline{\mathbf{k}}$, $\underline{\mathbf{v}} = 4\underline{\mathbf{i}} + 6\underline{\mathbf{j}} + 2\underline{\mathbf{k}}$ and $\underline{\mathbf{w}} = -6\underline{\mathbf{i}} - 9\underline{\mathbf{j}} - 3\underline{\mathbf{k}}$ then find $\underline{\mathbf{u}} + 2\underline{\mathbf{v}}$				
v	If $\underline{\mathbf{a}} = 2\underline{\mathbf{i}} - 2\mathbf{j} + 4\underline{\mathbf{k}}$, $\underline{\mathbf{b}} = -\underline{\mathbf{i}} + \mathbf{j} - 2\underline{\mathbf{k}}$ then find a unit vector perpendicular to plane				
	containing <u>a</u> and <u>b</u>				
vi	If $\underline{\mathbf{u}} = \underline{\mathbf{i}} + 2\underline{\mathbf{j}} - \underline{\mathbf{k}}$, $\underline{\mathbf{v}} = \underline{\mathbf{i}} - 2\underline{\mathbf{j}} + 3\underline{\mathbf{k}}$ and $\underline{\mathbf{w}} = \underline{\mathbf{i}} - 7\underline{\mathbf{j}} - 4\underline{\mathbf{k}}$. Then find volume of				
	parallelepiped by these vectors				
vii	Find work done, if the point at which the constant force $\underline{F} = 4\underline{i} + 3\underline{j} + 5\underline{k}$ is applied to an				
	object moves from $P_1(3,1,-2)$ to $P_2(2,4,6)$				
viii	Write equation of normal to the circle $x^2 + y^2 = 25$ at $(5 \cos \theta, 5 \sin \theta)$				
ix	Find focus of the parabola $x^2 - 4x - 8y + 4 = 0$				
х	Find eccentricity and vertices of the hyperbola $\frac{x^2}{16} - \frac{y^2}{9} = 1$				
xi	Define circle and write equation of circle in standard form				
xii	Find equation of the parabola with focus $(2, 5)$ and directrix $y = 1$				
xiii	Find centre and foci of the hyperbola $\frac{y^2}{4} - x^2 = 1$				

16

SECTION-II

Note: Attempt any Three questions from this section.

 $10 \times 3 = 30$

O 5- (A)	If x	$=\frac{1-t^2}{2}$. y=	2 t	,	then show	y	$\frac{dy}{dx} + x = 0$	

(B) Find m and n so that the given function is continuous at x = 3 if (mx) if x < 3

$$f(x) = \begin{cases} mx & \text{if } x < 3 \\ n & \text{if } x = 3 \\ -2x + 9 & \text{if } x > 3 \end{cases}$$

- Q.6- (A) Find $\int \sin^4 x \, dx$
 - (B) Find the equation of the line through (5, -8) and perpendicular to join of A(-15, -8), B(10, 7)
- Q.7-(A) Evaluate $\int_{-1}^{2} (x + |x|) dx$
 - (B) Maximize f(x,y) = x + 3y; subject to the constraints $2x + 5y \le 30$, $5x + 4y \le 20$, $x \ge 0$, $y \ge 0$
- Q.8-(A) Find the area of the region bounded by the triangle whose sides are 7x y 10 = 0; 10x + y 41 = 0; 3x + 2y + 3 = 0
 - (B) Determine the equations of tangents to the circle $x^2 + y^2 = 2$ perpendicular to the line 3x + 2y = 6
- Q.9-(A) By transforming the equation $x^4 + 4y^2 2x + 8y + 4 = 0$ referred to a new origin and axes remaining parallel to the original axes, the first terms are removed. Find the coordinates of the new origin and the transformed equation
 - (B) Prove that: $\cos(\alpha \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$

OBJECTIVE

NOTE: You have four choices for each objective type question as A, B, C and D. The choice which you think is correct, fill that circle in front of that question number. Use marker or pen to fill the circles. Cutting or filling two or more circles will result in zero mark in that question.

QUESTION NO. 1 DGK-52-20 $\lim_{n \to +\infty} \left(1 + \frac{1}{n}\right)^{\frac{n}{2}} = \dots$ (A) e^n (B) e (C) $e^{1/2}$ (D) $e^{-1/2}$ If f(x) = 2x + 1, $g(x) = \frac{3}{x-1}$ $x \ne 1$ then fog(x) = ...(A) $\frac{5+x}{x-1}$ (B) $\frac{3}{2x}$ (C) 4x + 3 (D) $\frac{3(x-1)}{4-x}$ $\frac{d}{dx} \cot h^{-1} x = \dots$ $\frac{d}{dx} \cot h^{-1} x = \dots$ (A) $\frac{1}{1-x^2}$ (B) $\frac{1}{x^2-1}$ (C) $\frac{1}{1+x^2}$ (D) $\frac{-1}{1+x^2}$ $\frac{d}{dx} (x+4)^{1/3} = \dots$ (A) $(x+4)^{-1/3}$ (B) $\frac{1}{3} (x+4)^{-1/3}$ (C) $\frac{1}{3} (x+4)^{-2/3}$ (D) $\frac{1}{3} (x+4)^{2/3}$ $\frac{d}{dx} e^{\sin x} = \dots$ (A) $e^{\sin x}$ (B) $\cos x e^{\sin x}$ (C) $\sin x e^{\sin x-1}$ (D) $-\cos x e^{\sin x}$ If f be a differentiable function on the open interval (a, b) then f is increasing function if \(\text{(A) f (x) < 0}\) (B) f (x) > 0 (C) f(x) \leq 0 (D) f (x) < 0 $\int \frac{1}{ax+b} dx = \dots$ (A) $\ln |ax+b| + c$ (B) $\frac{ax+b}{a} + c$ (C) $\frac{-a}{(ax+b)^2} + c$ (D) $\frac{1}{a} \ln |ax+b| + c$ 6 $\int (f(x))^{-1} f(x) dx = \dots$ (A) $\ln |f(x)| + c$ (B) $\frac{[(f(x))^{-1}]^2}{2} + c$ (C) $(f(x))^{-1} + c$ (D) f(x) + c $\int \tan^2 x \, dx = \dots$ (A) $\sec^2 x + c$ (B) $\sec^2 x - x + c$ (C) $x - \sec^2 x + c$ (D) $- \csc^2 x + c$ Solution of the differential equation $x \frac{dy}{dx} = 1 + y$ is 10 (B) ce^y (C) y = cx - 1 (D) $x^2 + y^2 = c$ Equation of horizontal line through (7, -9) is 11 (A) y = -9 (B) y = 9 (C) x = 7 (D) x = -712 Slope intercept form of the line 2x + y - 11 = 0 is (A) $\frac{x}{(11/2)} + \frac{\hat{y}}{11} = 1$ (B) y = -2x + 11 (C) y = 2x - 11 (D) y = -2x - 11If $\theta = 45^{\circ}$ be the inclination of the line with x-axis then slope of the line is 13 (B) $\frac{1}{\sqrt{2}}$ (C) -1 (D) 1 The equation $ax^2 + 2hxy + by^2 = 0$ represents a pair of orthogonal lines if (A) $h^2 - ab = 0$ (B) a + b = 0 (C) $h^2 + ab = 0$ (D) a - b = 014 15 The non-negative constraints used in a system of linear in equalities are called (A) Problem constraints (B) Decision variable (C) Feasible solution (D) Optimal solution Co-ordinate of the centre of the circle $x^2 + y^2 + 12x - 10y = 0$ is 16 (A) (6, -5) (B) (-6, -5) (C) (-6, 5) (D) (6, 5)Focus of the parabola $x^2 = -4ax$ is 17 (A)(0, -a)(B) (0, a) (C) (-a, 0)Equation of Directrices of Hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ (A) y = 0 (B) x = 0 (C) $y = \pm \frac{c}{e^2}$ (D) $x = \pm \frac{c}{e^2}$ 18 19 The value of $\begin{bmatrix} \underline{i} & \underline{i} & \underline{k} \end{bmatrix} = \dots$ (B) 0 (C) -1 (D) k20 With usual notations in any triangle ABC $c \cos A + a \cos c = .$ (A) a (C) c (D) 1 (B) b

12th CLASS - 12022 SUBJECTIVE SECTION-I

TIME: 2.30 HOURS MARKS: 80

QUESTION NO. 2 Write short answers any Eight (8) of the following DCK-92-22

i	If $f(x) = x^2 - x$, Evaluate $f(x-1)$
ii	Explain Identity function by example
iii	Evaluate $\lim_{x \to \pi} \frac{\sin x}{\pi - x}$
iv	Show that $x = a \cos t$ and $y = a \sin t$ are the parametric equation of the circle $x^2 + y^2 = a^2$
V	Express $\lim_{n \to +\infty} \left(1 + \frac{3}{n}\right)^{2n}$ in terms of e
vi	If $x = t^2 + 1$, $y = t^2$ find $\frac{dy}{dx}$
vii	If $3x + 4y + 7 = 0$ then find $\frac{dy}{dx}$
viii	Differentiate $\frac{1}{a} \sin^{-1} \frac{a}{x}$ w.r.t x
ix	Find y_2 if $x^2 + y^2 = a^2$,
Х	Explain increasing function and give its example
xi	Differentiate sin x w.r.t cot x
xii	Calculate $\frac{d}{d}$ (3 $x^{4/3}$)

 $\frac{|X|}{|X|}$ | Calculate $\frac{\pi}{dx}$ (3 $x^{4/3}$)

QUESTION NO. 3 | Write short answers any Eight (8) of the following

S	HON	NO. 3 Write short answers any Eight (8) of the following	16
	i	Evaluate $\int \frac{\cos 2x - 1}{1 + \cos 2x} dx$	
	ii	Evaluate $\int a^{x^2} x \ dx$	
	iii	Evaluate $\int \frac{dx}{\frac{1}{2}\sin x + \frac{\sqrt{3}}{2}\cos x}$	
	iv	Evaluate $\int (en x)^2 dx$	
	v	Find $\int_{-1}^{3} (x^3 + 3x^2) dx$	
	vi	If $\int_{-2}^{1} f(x) dx = 5$ and $\int_{-2}^{1} g(x) dx = 4$ Then evaluate $\int_{-2}^{1} (2f(x) + 3g(x)) dx$	
	vii	Find area between the x-axis and the curve $y = 4x - x^2$	
	viii	Check $y = \tan(e^x + c)$ is a solution of the differential equation of $\frac{dy}{dx} = \frac{y^2 + 1}{e^{-x}}$	
	ix	If the vertices of a triangular region are $A(5,3)$, $B(-2,2)$ and $C(4,2)$. Find its area	
	х	Convert $5x - 12y + 39 = 0$ into slope intercept and intercept form	
	xi	Find the point three-fifth of the way along line segment from A(-5, 8) to B(5, 3)	
	xii	By means of slope show that the points (4, -5), (5, 7) and (10, 15) lies on a same line	

 $\lfloor xii \rfloor$ By means of slope show that the points (4, -5), (5, 7) and (10, 15) lies on a same line QUESTION NO. 4 Write short answers any Nine (9) of the following

TION	NO. 4 Write short answers any Nine (9) of the following	18			
i	Graph the solution set of linear inequality $3y - 4 \le 0$ in $xy - plane$				
ii	Define feasible region and feasible solution				
iii	Find an equation of the circle with centre at $(\sqrt{2}, -3\sqrt{3})$ and radius $2\sqrt{2}$				
iv	Find the focus and directrix of the parabola $y^2 = -8(x-3)$				
v	Find an equation of the ellipse with foci (- $3\sqrt{3}$, 0) and vertices (± 6 , 0)				
vi	Find focus of the parabola $x^2 - 4x - 8y + 4 = 0$				
vii	Check the position of the point (5, 6) with respect to the circle $x^2 + y^2 = 81$				
viii	Find the centre and radius of the circle $4x^2 + 4y^2 - 8x + 12y - 25 = 0$				
ix	Write the vector \underline{PQ} in the form $x\underline{i} + y\underline{j}$ if $P(0, 5)$, $Q(-1, -6)$				
х	Find the sum of the vectors \underline{AB} and \underline{CD} given that four points				
	A(1,-1), B(2,0), C(-1,3), D(-2,2)				
xi	Find a unit vector in the direction of $\underline{V} = \underline{i} + 2\underline{j} - \underline{k}$				
xii	Find the cosines of angle θ between $\underline{U} = [2, -3, 1]$, $\underline{V} = [2, 4, 1]$				
xiii	Prove that $\underline{a} \times (\underline{b} + \underline{c}) + \underline{b} \times (\underline{c} + \underline{a}) + \underline{c} \times (\underline{a} + \underline{b}) = 0$				

SECTION-II

Note: Attempt any Three questions from this section

 $10 \times 3 = 30$

	09K-91-22
	Find $\lim_{\theta \to 0} \frac{\tan \theta - \sin \theta}{\sin^3 \theta}$ Prove that if $\frac{y}{x} = \tan^{-1} \frac{x}{y}$ then $\frac{dy}{dx} = \frac{y}{x}$
Q.6- (A) (B)	Evaluate $\int \frac{x + \sin x}{1 + \cos x} dx$ Find an equation of line through (-4, 7) and parallel to the line $2x - 7y + 4 = 0$
Q.7-(A) (B)	Evaluate $\int_0^{\pi/4} \frac{\sec \theta}{\sin \theta + \cos \theta} d\theta$ Graph the feasible region of the system of linear inequalities and find the corner points of $3x + 2y \ge 6$, $x + y \le 4$, $x \ge 0$, $y \ge 0$
Q.8-(A)	Find a joint equation of the straight lines through the origin perpendicular to the lines represented by $x^2 + xy - 6y^2 = 0$ Find equation of the tangent drawn from $(0, 5)$ to $x^2 + y^2 = 16$
Q.9-(A) (B)	Find the centre, foci, eccentricity, vertices and equations of directrices of $\frac{y^2}{4} - x^2 = 1$ Prove that: $\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$

118 (Sub) -12022 - 80000